2.11 Derivatives of Inverse Trigonometric Functions

①
$$\frac{d}{dx}[2x + \sin(2x^2) + 5] = 2 + \cos(2x^2) \cdot 4x$$

 $= 2 + 4x\cos(2x^2)$
② $\frac{d}{dx}(x^4y + 4y^3 = 10x) = [x^4)(y) + (y)(4x^3) + [2y^2 \cdot y] = 10$
 $x^4y' + 4x^3y + [2y^2y' = 10 - 4x^3y]$
 $y'(x^4 + [2y^2) = 10 - 4x^3y]$
 $y' = \frac{10 - 4x^3y}{x^4 + [2y^2]}$
③ $y = \cos^2(4x + 3) = (\cos 4x + 3)^2$
 $y' = 2(\cos(4x + 3)) \cdot (-\sin(4x + 3)) \cdot 4$
 $= -8\cos(4x + 3)\sin(4x + 3)$.

[Old Implicit Differentiation & Chain Rule

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Thew Inverse Trigmometric Function Derivatives · The inverse trig functions are sin-1x, cos-1x, tan-1x. please note. These do not mean 1 , 1 , 1 + these are reciprocal functions like cscx, secx & cotx. · Inverse Trig Functions are inverses of each trig functions. (For example) sin-1x -> means "inverse sine" where sin-1x is the angle whose sine is x. $Sin \theta = X$ $\theta = Sin^{-1}X.$ Sin y = X Sin x = y. Let's consider y= sin 1x. Derive the derivative. y=sin-1x So, $\sin y = x$. Then if we find the derivative: $\cos y \cdot y' = 1$ $y' = \frac{1}{\cos y}$ Since $y = \sin^{-1}x$, then $y' = \frac{1}{\cos(\sin^{-1}x)}$. Let $\theta = \sin^{-1}x$ Then $\sin \theta = x$ O $\sin \theta = \frac{x}{1}$ $x^2 + 7^2 = 1^2$ $7^2 = 1 - x^2$ This was created by Keenan Xavier Lee, 2013. See my website for more information, lee-apcalculus weebly com.

Now,
$$y' = \frac{1}{\cos \theta}$$
 & $\cos \theta = \frac{\sqrt{1-x^2}}{1}$.

Therefore $y' = \frac{1}{\sqrt{1-x^2}}$.

Let's consider $y = \tan^{-1}x$. Derive the derivative.

 $y = \tan^{-2}x$

So, $\tan y = x$.

Now, take the derivative:

 $\sec^2 y \cdot y' = 1$
 $y' = \frac{1}{\sec^2 y}$

Since $y = \tan^{-1}x$, $y' = \frac{1}{\sec^2(\tan^2x)}$.

Let
$$\theta = \tan^{-1}x$$
.

Background

Trig Identities

Then $\tan \theta = x$

Information

Sin^2x + cos^2x = 1

1 + $\tan^2 x = \sec^2 x$.

So $\sin \omega = 1 + \tan^2 x = \sec^2 x$.

 $y' = \frac{1}{1 + \tan^2 \theta}$

Furthermore, Since tan20

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(1)
$$f(x) = \sin^{-1}(x^{2})$$

 $f'(x) = \frac{1}{\sqrt{1 - (x^{2})^{2}}}$. $2x = 2x$
(2) $\frac{d}{dx} \operatorname{arc} \sin(3x^{2}) = \frac{1 - (3x^{2})^{2}}{9x}$
 $= \sqrt{1 - 9x^{4}}$
(3) $\frac{d}{dx} \operatorname{arc} \cos(\frac{1}{x}) = \frac{-1}{\sqrt{1 - (x^{2})^{2}}}$. $(-x^{-2})$
 $= \frac{1}{x^{2}\sqrt{1 - x^{-2}}}$

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 $\frac{d}{dx} \sin^{-1} x = \frac{1}{\sqrt{1 - (f(x))^2}} \cdot f'(x) \qquad \frac{d}{dx} \cos^{-1} x = \frac{-1}{\sqrt{1 - (f(x))^2}} \cdot f'(x)$

Derivatives of Inverse Tria Functions

 $\frac{d}{dx} \tan^{-1} x = \frac{1}{1 + (f(x))^2} \cdot f'(x)$

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· 1-7, 13, 21, 27,

Examples