

2.6 Solving System of Equations

Graphing

Standard:

A.REI.6



[Old] Graphing Linear Equations

Let's recall 2 forms for linear equations:

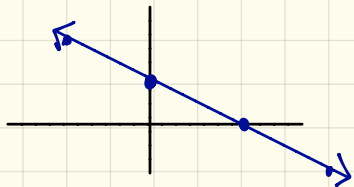
- slope-intercept form: $y = mx + b$ → best for graphing
- standard form: $ax + by = c$

$$y = mx + b$$

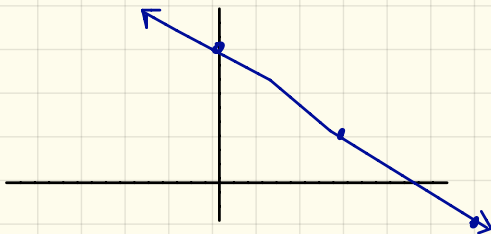
$m = \text{slope}$, $b = \text{y-intercept}$.

Graph Lines.

① $y = \frac{1}{2}x + 1$



② $-3x - 6y = 18$



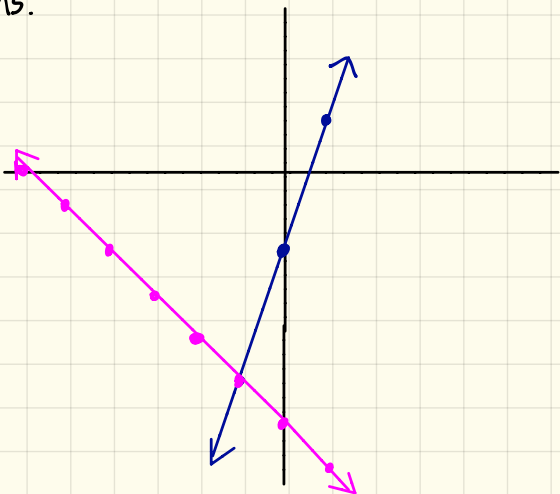
$$\begin{aligned} -4x - 6y &= 18 \\ \cancel{1x} + \cancel{1x} - 6y &= 4x + 18 \\ \frac{-6y}{-6} &= \frac{4x + 18}{-6} \\ y &= -\frac{2}{3}x - 3 \end{aligned}$$

[new] Solving Systems of Equations (Graphically)

A system of equations is a set or collection of equations that one deals with at one time (simultaneously).

Let's consider the 2 following equations.

— $y = 3x - 2$
— $y = -x - 6$



- [1] Graph the 2 equations.
- [2] Do they intersect? If so, where?

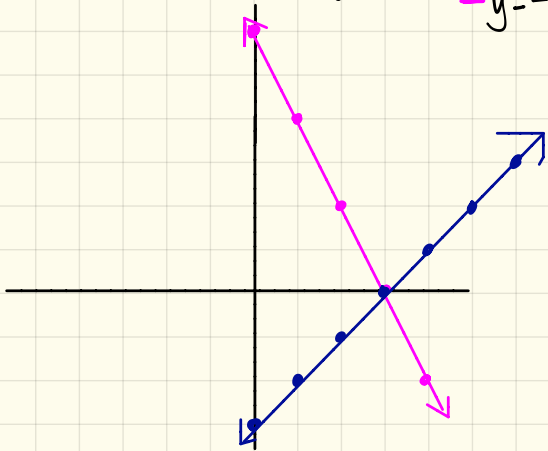
$(-1, -5)$.

Basic Idea of Solving System of Linear Equations

The goal is to find the point that marks the intersection of the 2 lines. The point that intersects on the graph is the solution to the system of linear equations.

[Example 1] Find the solution to the system.

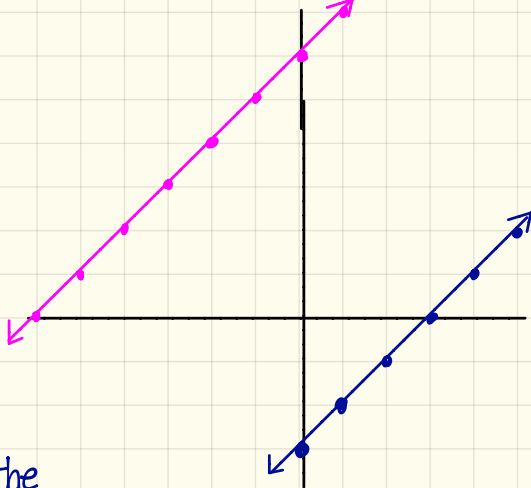
— $y = x - 3$
— $y = -2x + 6$



Solution: $(3, 0)$

Let's consider the 2 equations:

$$\begin{aligned} & \text{---} y = x - 3 \\ & \text{---} y = x + 6 \end{aligned}$$



- 1] Graph the 2 equations.
- 2] Do they intersect? If so, where?

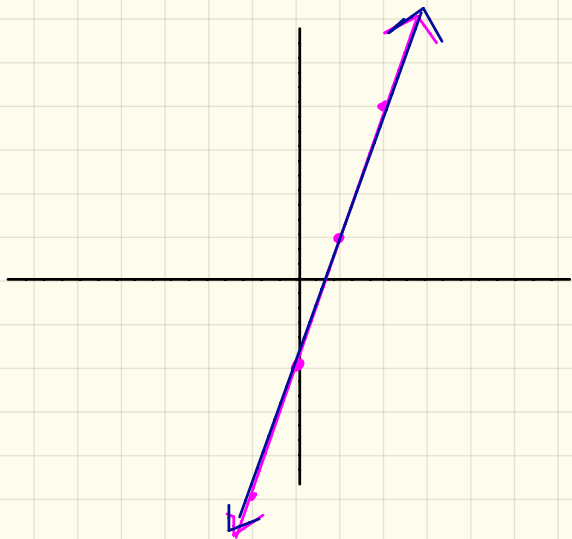
They do not intersect.

Why do they not intersect? What do the 2 equations have in common?

The 2 equations have the same slope, thus the lines will never cross & will remain parallel.

Let's consider the 2 equations:

$$\begin{aligned} & \text{---} y = 3x - 2 \\ & \text{---} y = 3x - 2 \end{aligned}$$



- 1] Graph the 2 equations.
- 2] Do they intersect? If so, where?

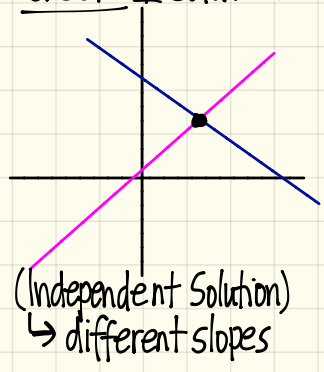
The 2 lines intersect at every point on the line.

Why do they intersect at every point? What do the 2 equations have in common?

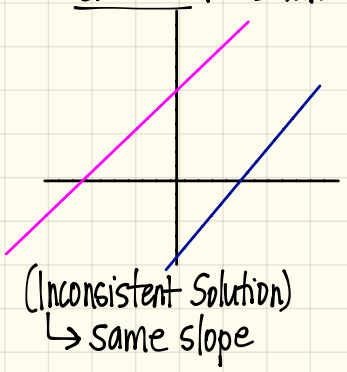
The 2 equations have the same slope and same y-intercept. Since they have they are the same equations, the 2 lines lie on top of one another, thus having an infinite amount of solutions.

Conclusion There are 3 possible solutions for solving systems.

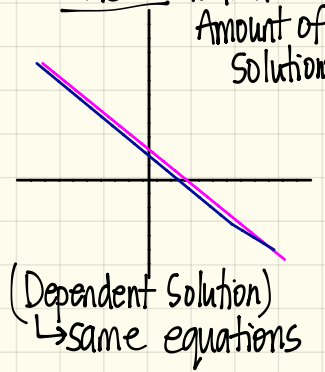
CASE A 1 solution



CASE B No solution

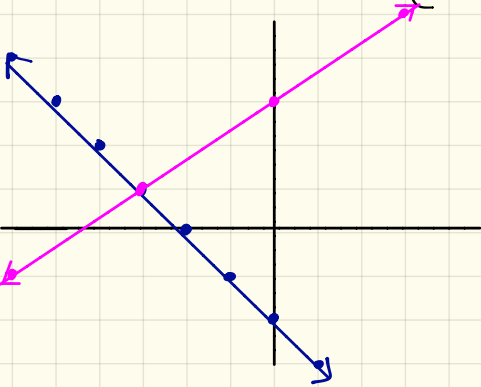


CASE C Infinite Amount of Solutions



[Example 1] Solve the system.

$$\begin{cases} y = -x - 2 & \text{---} \\ y = \frac{2}{3}x + 3 & \text{---} \end{cases}$$



Solution $(-3, 1)$

Check answer: $(-3, 1)$
 $x = -3, y = 1$

$$\begin{aligned} 1 &= -(-3) - 2 \\ 1 &= 3 - 2 \\ 1 &= 1. \checkmark \end{aligned}$$

$$\begin{aligned} 1 &= \frac{2}{3}(-3) + 3 \\ 1 &= -2 + 3 \\ 1 &= 1. \checkmark \end{aligned}$$

[More Examples] Determine whether the ordered pair is a solution of the system.

$$\begin{array}{l} 3x + 2y = 4 \\ -x + 3y = -5 \end{array} \quad (2, -1).$$

$$3(2) + 2(-1) = 4$$

$$6 + -2 = 4$$

$$4 = 4 \checkmark$$

$$-(2) + 3(-1) = -5$$

$$-2 + -3 = -5$$

$$-5 = -5 \checkmark$$

$(2, -1)$ is the solution to the system.