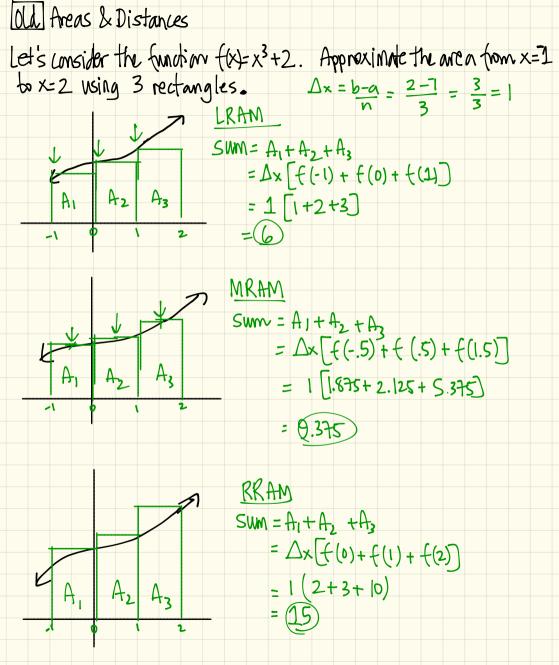
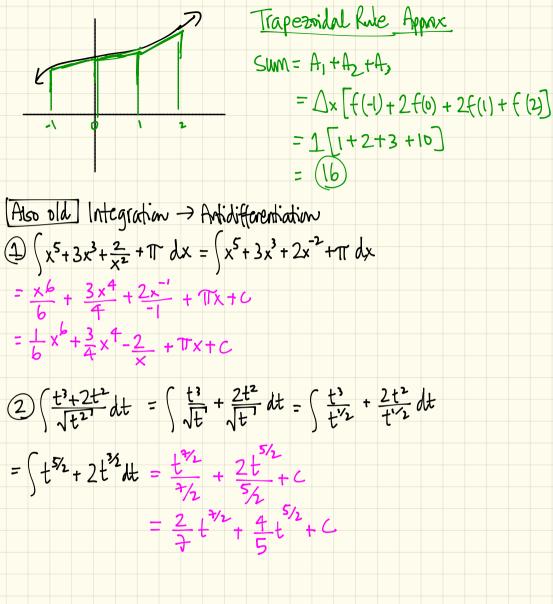
4.3 The Fundamental Theorem of Calculus

| Standards: | |
|------------|--|
| MCI1 | |
| MCI1b | |
| | |





[New] The FTC
Let's consider a function of continuous on
$$[a, b]$$
.

$$y = f(t)$$

$$f'(x) = \frac{d}{dt} \quad (f(t) \, dt = f(x))$$

$$a \times b \quad T \cdot Every continuous (has an antidorivative f(x))$$

$$F(x) = \int_{a}^{x} f(t) \, dt, \text{ where } x \text{ is } in (a, b) \quad w \text{ integration}.$$

$$F(x) = \int_{a}^{x} f(t) \, dt, \text{ where } x \text{ is } in (a, b) \quad w \text{ integration}.$$

$$\frac{Def(nihi m)}{f + f \text{ is continuous on } [a, b] \text{ then}, \quad F(x) = \int_{a}^{x} f(t) \, dt, \quad a \le x \le b.$$

$$F(x) = \int_{a}^{x} f(t) \, dt, \text{ othere } x \text{ is } in (a, b) \quad w \text{ integration}.$$

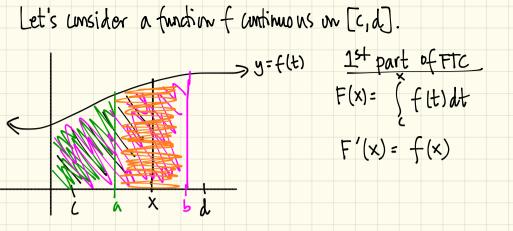
$$\frac{Def(nihi m)}{f + f \text{ is continuous on } [a, b] \text{ then}, \quad F(x) = \int_{a}^{x} f(t) \, dt, \quad a \le x \le b.$$

$$F(x) = \int_{a}^{x} f(t) \, dt \text{ erivatives.}$$

$$f(x) = \int_{a}^{x} f(t^{2} - 1)^{20} \, dt = (x^{2} - 1)^{20}$$

(2) $f(x) = \int_{x}^{x} \frac{\cos^{2} t}{\ln(t - \sqrt{t})} dt$ $f'(x) = \frac{d}{dt} \left(\frac{\cos^2 t}{1 - \sqrt{t}} \right) dt = \frac{\cos^2 x}{\ln(x - \sqrt{x})}$

Sometimes you might have to use the chain rule .. (f) $h(x) = \int_{0}^{x^{2}} \omega t^{2} t dt$ $\frac{\pi}{h'(x)} = \frac{d}{dx} \int_{\pi}^{x^{2}} \cot^{2}t \, dt = \cot^{2}(x^{2}) \cdot 2x$ $= 2x \omega t^{2}(x^{2}).$



Let's think about what: (assuming b > a) $F(b) - F(a) = \int f(t) dt - \int f(t) dt = \int f(t) dt$

 $\frac{2^{nd} \text{ part of FTC}}{\left[f(x) dx = F(x)\right]^{b}} = F(b) - F(a) \text{ where } F' = f.$ (so where F is the antiderivalive off)

