5.3 Volumes of Solids of Revolution Disk Method

Standards:	
MC11	
MC11c	
	1

Let's consider $f(x) = x^2 - 4x + 10 & g(x) = 4x - x^2$. Find the area of region between x=1 & x=3.

$$\frac{f(x)=x^{2}-4x+10}{3}$$

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$$= \int_{0}^{2} 2x^{2} - 8x + 10 dx$$

$$= \frac{2x^{3}}{3} - \frac{8x^{2}}{2} + 10x = \frac{2}{3}x^{3} - 4x^{2} + 10x = \frac{3}{3}$$

$$= \left[\frac{2}{3}(3)^3 - 4(3)^2 + 10(3)\right] - \left[\frac{2}{3}(1)^3 - 4(1)^2 + 10(1)\right] =$$

$$=$$
 $\left(\frac{26}{3}\right)$

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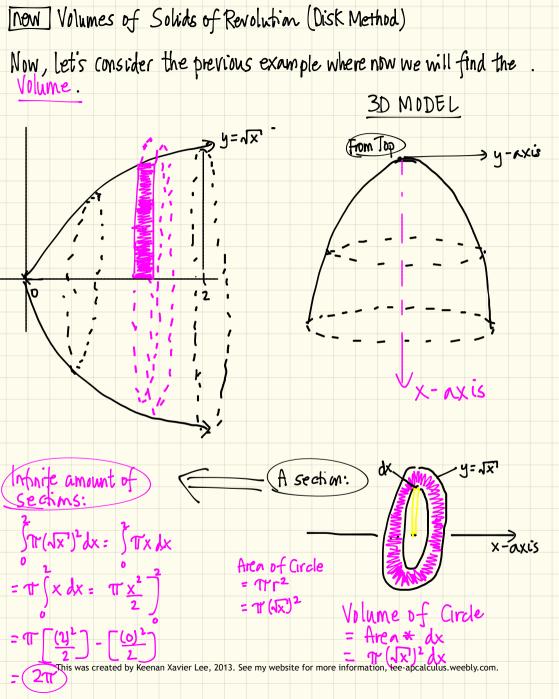
2nd Practice problem:
$$f(x) = \sqrt{x}$$
, $0 \le x \le 2$, find the area.

$$\int_{0}^{2} (\sqrt{x^{2}} - [0]) dx$$

$$= \int_{0}^{2} x^{2} dx$$

$$= \left[\frac{2}{3}(2)^{2}\right] - \left[\frac{2}{3}(0)^{2}\right]$$

$$= \frac{2}{3}\sqrt{2^{3}} - \frac{2}{3}\sqrt{0^{3}}$$



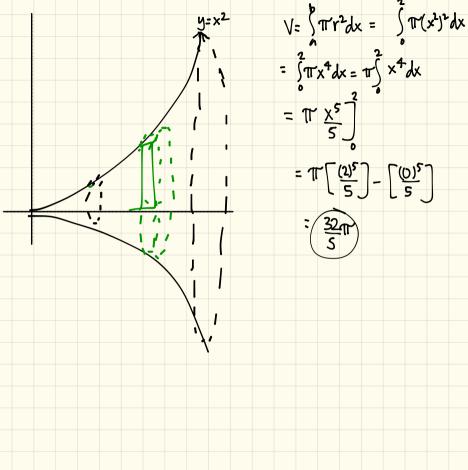
So let's generalize! Let's consider a curve y=f(x) & find the volume revolving around x-axis. 1 y-axis y= (K) X-axis 4= f(x) A section A= 1712 = 17(+(x))2 V= A* dx = T(f(x1)2dx "Take the sum of ALL OF THE DISKS"

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Formula when revolving around x-axis

Volume= ST (f(x)) dx

[Example 1] Find the volume of the solid by revolving around x-axis of y=x², y=0 and x=2.



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